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Environ. Sci. Technol., Just Accepted Manuscript • DOI: 10.1021/acs.est.9b02513 • Publication Date (Web): 03 Oct 2019

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Abstract

Business aviation is a relatively small but steadily growing and little investigated emissions source. Regarding emissions, aircraft turbine engines rated at and below 26.7 kN thrust are certified only for visible smoke and are excluded from the non-volatile particulate matter (nvPM) standard. Here, we report nvPM emission characteristics of a widely used small turbofan engine determined in a ground test of a Dassault Falcon 900EX business jet. These are the first reported nvPM emissions of a small in-production turbofan engine determined with a standardized measurement system used for emissions certification of large turbofan engines. The ground level measurements together with a detailed engine performance model were used to predict emissions at cruising altitudes. The measured nvPM emission characteristics strongly depended on engine thrust. The geometric mean diameter increased from 17 nm at idle to 45 nm at take-off. The nvPM emission indices peaked at low thrust levels (7% and 40% take-off thrust in terms of
nvPM number and mass, respectively). A comparison with a commercial airliner shows that a business jet may produce higher nvPM emissions from flight missions as well as from landing and take-off operations. This study will aid the development of emission inventories for small aircraft turbine engines and future emission standards.

**TOC art / graphical abstract**

![Graphical abstract]

**INTRODUCTION**

As the demand for air travel surges, fuel burn from commercial aviation is expected to double in the next 15 years.\(^1\) Thus, aircraft engine emissions will also increasingly affect climate and air quality. Commercial aviation accounts for approximately 2% of global man-made CO\(_2\) emissions.\(^2-\)\(^4\) Besides CO\(_2\) and water vapor, aircraft engines also emit gaseous pollutants (NO\(_x\), SO\(_x\), CO, unburned hydrocarbons (HC)) and soot. Soot is composed mostly of light absorbing carbon (black carbon, BC). In the aircraft jet engine emission standard, BC is reported as non-volatile particulate matter (nvPM; particles that are solid at the engine exit plane that do not volatilize when heated to 350 °C).\(^5,\)\(^6\) Aviation nvPM emissions absorb solar radiation, affect cloud formation, and deteriorate air quality at airports and in nearby communities.\(^3,\)\(^4,\)\(^7-\)\(^11\) Due to their potential health and climate impacts, various research programs have focused on characterization of particle emissions from aircraft engines, development of measurement
techniques and predictive models for estimating aviation nvPM emissions. Recent research has been motivated also by the development of a certification standard for nvPM emissions of new commercial aircraft turbine engines. The International Civil Aviation Organization (ICAO) has adopted the nvPM standard that applies to all engine types rated >26.7 kN thrust in production on or after 1 January 2020. In the longer term, regulatory limits for nvPM number as well as nvPM mass emissions are expected to be enforced. However, since small engines are excluded from the nvPM standard, nvPM emissions of business jets remain largely unknown.

Similar to commercial aviation, business aviation has flourished. The fleet is predicted to grow worldwide by 33% in the next 8 years. Although business aviation consumes only around 2% of the world’s jet fuel, small engines used on business aircraft may produce high nvPM emissions relative to their fuel burn due to technical and economic reasons and lack of emission regulations. Small engines rated ≤ 26.7 kN thrust are regulated for visible smoke only via the smoke number (SN). Moreover, the certification SN data for these engines are not part of the publicly available ICAO emissions databank. Thus, although methods for estimating nvPM emissions from SN have been developed, their applicability to small turbine engines (turboprop and turboshift as well as turbofan) is limited and ambiguous. To date, no nvPM emission indices (EI; amount of pollutant per kg fuel burned) have been reported for unregulated small turbine engines using the methodology used for emissions certification of large turbofan engines. Previously, nvPM EIs of a widely used turboprop have been reported from exhaust samples taken 10–15 m behind the aircraft’s tail using a simplified sampling system. The regulatory nvPM measurement system has been demonstrated on a small turbofan engine in a study of fuel composition effects on nvPM emissions, but no EIs have been reported.
Here, we report nvPM emission characteristics of a widely used small turbofan engine measured at ground level and modeled for cruising altitudes. We measured gaseous and nvPM emissions from a Honeywell TFE731-60 turbofan engine on a Dassault Falcon 900EX aircraft. We deployed the Swiss Mobile Aircraft Engine Emissions Measurement System (SMARTEMIS), which serves as a global reference system for the regulatory nvPM measurements. We report the EIs of nvPM number and mass as well as particle size distributions at ground level as a function of thrust from ground idle to take-off. We calculated nvPM emissions from the standardized landing and take-off cycle (LTO), which consists of four static thrust levels that approximate airport operations under 3000 ft (900 m) above ground: taxi (7% thrust), approach (30% thrust), climb-out (85% thrust), and take-off (100% thrust). We also developed a detailed engine performance model to estimate nvPM emissions at cruising altitudes and compared the emission estimates with previous studies of commercial airliners.

**MATERIALS AND METHODS**

**Engine emission tests.** The emission measurements were performed in a static ground-level test of the central engine of a Dassault Falcon 900EX (Figure 1). The engine was fueled with military-grade JP-8 fuel, which has nearly the same specifications as the commercial Jet A-1 but contains the following additives: a lubricity enhancer (0.1% mass), an icing inhibitor (0.1% volume), and a static dissipater (ppm level). The fuel batch used fulfilled the requirements for the fuel used in aircraft turbine engine emission testing according to Appendix 4 of the ICAO Annex 16 Vol. II. The weather during the test was dry and sunny with a temperature range from 11.2 °C to 20.2 °C, relative humidity between 40% and 70% and ambient pressure in the range from 96.5 kPa to 96.8 kPa. The engine test consisted
of a warm-up sequence and 11 test points on a descending power curve from take-off to idle (S2 in the SI). The engine was kept at each condition typically for 3 minutes (depending on the emissions stabilization time). The engine test was run three times on the same day. We used the low-pressure rotor speed (N1; rotational speed of the low pressure compressor and turbine) for setting the engine test points, using a correlation of thrust with N1 for the international standard atmosphere (ISA) conditions at sea level (15 °C and 101.325 kPa) provided by the engine manufacturer. The N1 settings could be repeated within 0.5% for all points except for maximum thrust, which was set by pushing the thrust lever to take-off position. The required take-off thrust set by the engine controller is typically below the maximum rated value and it varies with aircraft weight and ambient conditions. The average N1 from the three test runs at take-off was 98% (range 97.3%–98.7%), corresponding to ~95% of the rated sea level thrust. Common for small turbofan engines, the engine had an exhaust mixer, which mixed the hot core exhaust gases and the cold bypass air in a common nozzle. The mixed exhaust samples were extracted ~30 cm downstream of the engine exhaust nozzle exit plane (a plane perpendicular to the engine center line at the exhaust nozzle exit) with a sampling probe made of Inconel 600 alloy. The probe had a cruciform design with 12 orifices that provided a representative exhaust gas sample according to the smoke emissions certification standard.\(^5\)
Figure 1 Schematic of the experimental setup for the emission tests on the center engine of the Dassault Falcon 900EX done with SMARTMIS.

SMARTMIS connected to the probe is compliant with the new nvPM emissions certification standard and was described in detail previously\textsuperscript{18,20,22,31}. Briefly, the probe was connected to a 5.5 m-long stainless steel tubing heated to 160°C and with an inner diameter (ID) of 8 mm. At the inlet of the diluter assembly, the sample was split into the pressure control line, the nvPM transfer section, and the raw gas line. The raw gas line (160°C, length 25 m, 6 mm ID,
flow of 18 slpm, carbon-filled polytetrafluoroethylene (PTFE)) transported the raw exhaust sample to the gas and smoke analysis system (CO₂, CO, NOₓ, SO₂, HC and SN). In the diluter assembly, a Dekati DI-1000 ejector diluter diluted the raw gas sample with dry synthetic air by a factor of ~8. The diluted sample was drawn through a trace-heated line (60°C, length 25 m, 8 mm ID, flow of 25 slpm, carbon-filled PTFE) to the particle instrumentation. The latter determined the nvPM number concentration of particles > 10 nm (AVL Particle Counter Advanced, AVL APC), the nvPM mass concentration (AVL Micro Soot Sensor, AVL MSS Model 483), and the particle size distribution (Scanning Mobility Particle Sizer, TSI SMPS Model 3938). All the particle instruments were factory-calibrated prior to the measurement campaign. The size distribution measurement is not required by the ICAO nvPM standard; however, it provides information relevant for health and climate effects studies. In the context of the nvPM mass and number measurement, size distribution measurements help to explain the relationship between nvPM mass and number concentrations and are important for an accurate sampling system loss correction.

**Particle loss correction.** All data presented here are corrected for particle loss to the inner walls of the sampling system, which is a significant artifact in gas turbine exhaust sampling. The main particle loss mechanisms are diffusion due to the long sampling lines (~34 m from probe inlet to the instrument inlet), and thermophoresis due to a temperature gradient between the exhaust gas and the sampling line wall. The thermophoretic loss for the engine tested was negligible due to its mixed-flow exhaust nozzle that diluted the hot core exhaust flow with the cold bypass air upstream of the sampling probe (the modeled highest mixed gas temperature was ~200 °C, the line temperature was held at 160°C). The size-dependent diffusional losses were calculated using the measured particle size distributions (PSD) and a modeled penetration function for the
sampling system. The size-dependent system penetration functions were calculated according to a standardized method developed for the aircraft engine nvPM testing published in the SAE Aerospace Recommended Practice (ARP) 6481. The PSD measured was divided by the system penetration function for the SMPS (exhaust probe inlet to SMPS inlet) to obtain the PSD at the engine exit plane. The exit plane PSD, both number and mass-based, were then fitted with lognormal distributions. The mass distributions were obtained by assuming an average particle density of 1 g/cm³ independent of thrust and particle size. Effective density of aircraft engine soot is particle size and thrust dependent, however, measurements have shown that the average density (mass / volume of the PSD) is nearly constant as a function of thrust and geometric mean diameter (GMD). Finally, the distributions at the engine exit plane were multiplied by the penetration functions from the sampling probe inlet to the inlets of the corresponding nvPM instruments. The nvPM number concentration was also corrected for the losses in the instrument (losses in the volatile particle remover and the counting efficiency cut-off). The resulting correction factors are the ratios of the integrated PSD at the engine exit plane to the PSD at the instrument inlets for mobility diameters ≥ 10 nm. The number-based correction factors were in the range 2–6 (i.e., 2- to 6-fold losses) and the mass-based correction factors were in the range 1.2–1.4 (i.e., 20%–40% losses) (S3 in the online SI).

**Emission indices.** The nvPM EIs were calculated using one-minute averages of the nvPM mass and number, CO, CO₂, HC, and NOₓ concentrations and the complete nvPM EI equations, which include a correction for ambient background residual nvPM. This correction may be required because in the mixed-flow engine configuration the ambient air dilutes the core flow upstream of the sampling probe. Without considering the ambient background nvPM, the nvPM EIs may be overestimated. For the worst-case scenario encountered in the ambient air checks pre- and post-
test (ambient nvPM mass 3.5 µg/m³ and 8000 particles/cm³), the effect of the ambient background nvPM on the nvPM EIs was <5% for nvPM mass and <1% for nvPM number and it was the highest at idle. The relative uncertainty (95% confidence) of the loss-corrected EIs was estimated to be 20% (propagation of the systematic and random errors in the EIs and particle loss correction). The loss-corrected nvPM EIs were then interpolated as a function of sea-level static thrust using 6th order polynomials. The interpolated EIs and fuel flow were used to calculate the LTO cycle emissions, which are simplified estimates of emissions from airport operations < 915 m (3000 ft) above ground level. To calculate the standard LTO emissions, the EI in each mode is multiplied by fuel flow and the mode duration (26, 4, 2.2, and 0.7 minutes for taxi, approach, climb-out, and take-off, respectively).5

**Emission estimates at cruising altitude.** We calculated the nvPM emissions at cruise Mach number of 0.8 at the reference cruising altitude of 35,000 ft (flight level (FL) 350) in the international standard atmosphere (ISA) at temperatures ISA ± 10 °C, and at Mach 0.8 at FL400 (ISA) at maximum cruise thrust according to the engine manufacturer’s specifications. To estimate the combustion-relevant engine parameters at these conditions, we developed a detailed calibrated engine performance model using the GasTurb 13 software package.34 The model provides the combustor inlet pressure (P3), temperature (T3) as well as the combustor exit air-fuel ratio (AFR) needed for correcting the reference mass emission indices (EIₘ) at ground (EIₘ at the same T₃ as at cruise) using known empirical equations.31,35 The number emission indices (EIₙ) at cruise were calculated from the ratio EIₙ/EIₘ as a function of T₃, which is based on the assumption that the GMD is a function of T₃.31,36 We compared the results of this method with a more elaborate one that estimates the cruise nvPM EIs from nvPM mass concentration, PSD properties (GMD and geometric standard deviation, GSD) and engine performance at cruise (see
RESULTS AND DISCUSSION

Particle size distribution characteristics. The PSD characteristics depended strongly on engine thrust (Figure 2). The GMD was smallest at idle (~17 nm), followed by an initial steep increase up to ~40% thrust. After this point, there was negligible further increase in size with increase in thrust. The largest size was observed at take-off thrust (~45 nm). The GSD of the measured PSD ranged from 1.85 to 1.95 (mean value for all test points was 1.91) independent of thrust. The PSD followed the lognormal distribution best at idle (R²=0.99) and departed from lognormality with increasing thrust (R²=0.95 at take-off). The GMD increase with engine thrust is consistent with previous emission measurements directly behind turbofan engines with conventional (single annular) combustors.\textsuperscript{18,19,29,31,37–39} However, Figure 2b shows that compared to a common large turbofan engine CFM56-7B, the GMD was larger at all thrust levels. As the GMD increased with thrust, the particle concentration increased as well from idle up to ~30% thrust, but it decreased with further increase in thrust with the minimum at take-off (Figure 2a). Similar PSD characteristics have not been reported for a commercial turbofan engine before. Previous studies found the largest GMD at engine conditions that produced the highest nvPM mass emission indices for staged combustor engines as well as for single annular combustor engines. For single annular combustor engines (most engines in service), this occurs typically at take-off thrust\textsuperscript{14,18,29,31,38,39}. Our results corroborate that the GMD of nvPM produced by jet engines with unstaged combustors increases with engine thrust (or T3) and it does not necessarily correlate with the nvPM mass concentration in the exhaust.\textsuperscript{31} We note that the concentrations of the PSDs
in Figure 2a have not been corrected for the bypass air dilution. The bypass air dilution does not affect the calculated emission indices, which were used in further analysis.

**Figure 2** Particle size distributions at the engine exit plane (mixed flow nozzle, no bypass dilution correction) at four thrust levels used for the LTO cycle calculation (a) and geometric mean diameter as a function of rated thrust, $F_{\text{oo}}$ (b). Shaded area in (b) represents the standard error of the fit (95% confidence). The error bars (95% confidence) for the LTO points are the combined uncertainties of the random standard uncertainty (standard deviation of the mean, $N=3$) and the total uncertainty in the GMD (5%). The curve from Durdina et al. (2017)\textsuperscript{31} is for the exit plane of a CFM56-7B engine (Boeing 737-800).
**Emission indices.** The emission indices of nvPM mass and number varied with engine thrust by more than an order of magnitude and peaked at low thrust levels (Figure 3). The EI$_m$ peaked at ~40% thrust and was the lowest and similar in magnitude at take-off and idle (Figure 3a). In contrast, the EI$_n$ peaked near idle power (~7% rated thrust) and decreased steadily with increasing thrust with a minimum at take-off (a factor of ~19 lower than at idle; Figure 3b). Such nvPM EI characteristics have not been reported for a commercial turbofan before. Typically, the EI$_m$ of turbofan engines of various sizes with conventional combustors increases with thrust with a maximum at or near take-off: $^{20,29,31,38,40}$ The EI$_n$ often follows an S-shaped curve with a maximum at idle, minimum at ~20% thrust, and further increase with thrust with a plateau at mid-range to maximum thrust (see gray lines in Figure 3 for comparison with a previous study of the CFM56-7B turbofan engine used on the Boeing 737-800$^{31}$).

Most importantly, the measured nvPM EIs not only had different thrust dependence than the widely used CFM56-7B engine, but they also differed strongly in magnitude for most of the engine conditions. The EI$_m$ was higher by a factor of ~200 at 30% thrust (approach mode in the LTO cycle); whereas at take-off, it was up to a factor of 2 lower (Figure 3a). The EI$_n$ was higher by up to a factor of 30 at taxi and approach thrust, whereas at take-off power it was up to a factor of 3 lower than found in the previous study for the airliner engine (Figure 3b). The relatively high nvPM EIs at low thrust compared to a conventional large turbofan engine indicate that a small aircraft with nvPM emission characteristics as reported here may be a significant nvPM source during low thrust operations (idle, taxiing, approach and landing) despite its lower fuel burn.
Figure 3 Emission indices (particle loss corrected) of nvPM mass (a) and nvPM number (b) as a function of thrust. The shaded areas are standard errors of the fits (95% confidence). The error bars (95% confidence) for the LTO points are the combined uncertainties of the random standard uncertainty (standard deviation of the mean, N=3) and the total uncertainty in the measured EIs (20%). The data from Durdina et al. (2017)\textsuperscript{31} are for the CFM56-7B26 engine (Boeing 737-800).

Note that the two studies compared here used different fuels, which affected the nvPM emissions. The fuel hydrogen mass content, which has been used as the correlating parameter for fuel effects on nvPM emissions\textsuperscript{19,20,41,42}, was 13.5% compared to Durdina et al. (2017)\textsuperscript{31} who used fuel with 14.3%. Fuels with higher hydrogen content burn cleaner and the effect on nvPM...
decreases with increasing engine thrust.\textsuperscript{19,20,42} According to the predictive model of Brem et al.\textsuperscript{20}, the difference between the nvPM EIs for two fuels with hydrogen mass content difference of 0.5\% (maximum range in their study) is \textasciitilde50\% at 30\% thrust and \textasciitilde5\% at take-off thrust. Nevertheless, the fuel used here is within the specifications for certification fuel and its lower hydrogen content is representative of fuel used in North America.\textsuperscript{43}

Another source of variability in nvPM emissions is ambient conditions. The variation in the measured EIs shown in Figure 3 (coefficient of variation 2–15\%) for a given thrust level is dominated primarily by the ambient temperature variability. As the ambient temperature varied, the combustor conditions for a given N1 varied with changes in air density, which affected the nvPM emissions measurably. Negative correlation of nvPM emissions with ambient temperature has been observed before\textsuperscript{18}, but no corrections for ambient effects have been developed yet. As the mean ambient temperature in the three runs was \textasciitilde15\textdegree C and the pressure was near standard sea level pressure, the interpolated EIs can be considered representative for sea level standard conditions.

\textbf{LTO cycle emissions.} The LTO cycle emissions were dominated by the taxi and approach modes (Figure 4). This is a result of the peak nvPM emissions at low thrust (Figure 3) and the longest times in those LTO modes (Table 1). The taxi and approach modes together constituted 71\% of the total nvPM mass and 95\% of the total nvPM number. This finding contrasts the LTO cycle emissions of a Boeing 737-800 (and other airliners), which are dominated by the climb and take-off modes.\textsuperscript{31} In comparison, the nvPM emissions from the taxi and approach modes of the Boeing 737-800 made up only 3\% of the total nvPM mass and 33\% of the total nvPM number. Interestingly, the total LTO emissions were higher than those of the airliner. The nvPM mass
was higher by 22% and the nvPM number was higher by a factor of 2. Thus, a business jet may be an important contributor to local air pollution, depending on the actual LTO operations.

We note that the certification LTO cycle likely overestimates emissions compared to a performance-based LTO model, but it is valuable for comparing emissions performance of different engines. The certification LTO cycle is meant to be an approximation, thus the thrust levels as well as the times in mode may be overestimated, especially for small airports serving private aviation. However, a low-emitting engine in the certification LTO cycle is expected to have good emissions performance also in the real world. To evaluate emissions performance of different engines from certification data, the total LTO cycle emissions are normalized to rated take-off thrust. The TFE731-60 engine (rated thrust 22.24 kN) produced 486 mg/kN and $1.7 \times 10^{16}$ particles/kN, whereas the CFM56-7B26 (rated thrust 117 kN) from the previous study of Durdina et al. (2017) emitted 113 mg/kN and $2.67 \times 10^{15}$ of particles/kN. Therefore, the smaller engine investigated here is expected to have worse nvPM emissions performance from LTO operations than the larger engine.
Figure 4 LTO cycle emissions of nvPM mass (a) and nvPM number (b) calculated per aircraft.

Table 1 Summary of the LTO emission indices, nvPM mass and number emissions per aircraft and geometric mean diameters (± estimated uncertainties at 95% confidence).

<table>
<thead>
<tr>
<th>LTO mode</th>
<th>LTO time in mode (s)</th>
<th>EI_m ± u_{95} (mg/kg)</th>
<th>EI_n ± u_{95} (#/kg)</th>
<th>nvPM mass per aircraft ± u_{95} (g)</th>
<th>nvPM number per aircraft ± u_{95} (#)</th>
<th>GMD ± u_{95} (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>taxi</td>
<td>1560</td>
<td>57.4 ± 13.5</td>
<td>5.7 \times 10^{15} ± 1.5 \times 10^{15}</td>
<td>8.5 ± 2</td>
<td>8.4 \times 10^{17} ± 2.2 \times 10^{17}</td>
<td>21.8 ± 1.4</td>
</tr>
<tr>
<td>approach</td>
<td>240</td>
<td>217.2 ± 61.5</td>
<td>3.4 \times 10^{15} ± 9.3 \times 10^{14}</td>
<td>14.8 ± 4.2</td>
<td>2.3 \times 10^{17} ± 6.4 \times 10^{16}</td>
<td>36.2 ± 1.9</td>
</tr>
<tr>
<td>climb-out</td>
<td>132</td>
<td>72 ± 26</td>
<td>4.7 \times 10^{14} ± 1.2 \times 10^{14}</td>
<td>7.1 ± 2.6</td>
<td>4.7 \times 10^{16} ± 1.2 \times 10^{16}</td>
<td>44.3 ± 3.4</td>
</tr>
<tr>
<td>take-off</td>
<td>42</td>
<td>59.6 ± 24.2</td>
<td>2.9 \times 10^{14} ± 1.8 \times 10^{14}</td>
<td>2.1 ± 0.9</td>
<td>1.0 \times 10^{16} ± 6.2 \times 10^{15}</td>
<td>45.5 ± 3.0</td>
</tr>
<tr>
<td>total</td>
<td></td>
<td></td>
<td></td>
<td>32.5 ± 5.4</td>
<td>1.1 \times 10^{18} ± 2.3 \times 10^{17}</td>
<td></td>
</tr>
</tbody>
</table>
Cruise emissions. The estimated nvPM EIs at cruising altitudes are shown in Figure 5. For the reference flight level of 35,000 ft (10.67 km) in ISA, the $E_{I_n}$ was $7.4 \times 10^{14}$ particles/kg of fuel burned, comparable with the previous modeling study for the Boeing 737-800.\textsuperscript{31} In contrast, the $E_{I_m}$ was 82 mg/kg of fuel burned, which is a factor of ~8 higher than found for the Boeing 737’s engines for the same flight conditions and using the same measurement system and modeling approach. This is due to the larger mean particle size. We estimated the GMD to be ~42 nm (compared to 22 nm for the Boeing 737), which means that the particle mass distribution is dominated by a fewer larger particles.

The nvPM EIs decreased with increasing ambient temperature. As ambient temperature increases, the engine runs at higher N1 at the same Mach number to compensate for the lower air density. The T3 increases, which, due to the nvPM emission characteristics of the engine studied (Figure 3), leads to decreasing nvPM EIs. Therefore, flying at higher altitudes and at maximum cruise thrust would result in lower nvPM emissions. This result contrasts the findings of previous studies of commercial turbofan engines with maximum nvPM mass emissions at maximum thrust.\textsuperscript{31,44} Overall, our estimated cruise nvPM mass emissions (82 mg/kg), which are most relevant for the direct radiative forcing effects, are higher than literature values used for the fleet average (25–40 mg/kg).\textsuperscript{3,45} Despite the small aircraft size and relatively low fuel burn, the nvPM mass emission rates were up to a factor of 3 higher than previously reported for the Boeing 737 engines (Figure 5c).
Figure 5 Emissions at cruise: EI of nvPM mass (a) EI nvPM number (b) nvPM mass per hour (c) and nvPM number per hour (d). The results for the DC-8-72 were obtained from exhaust plume sampling at cruise behind the aircraft flying at maximum range thrust burning medium- and low sulfur Jet A-1 fuel. The results for the Boeing 737-800 were modeled using an engine performance model and ground test data of the CFM56-7B engine.

**Implications.** Business jets are so far not accounted for accurately in emission inventories and have also been excluded from the certification requirements for nvPM emissions as well as for gaseous emissions. We have shown here that a modern business jet may emit as much nvPM from airport operations as an airliner. Also, the comparison with airliners at the cruising altitude suggests that nvPM emissions from a business jet flight may be higher than those of an airliner.
The thrust dependence of nvPM mass emissions of the engine investigated differed from those of large turbofan engines, on which predictive models are based. Models that predict aviation nvPM mass emissions at ground level and cruising altitude\textsuperscript{16,17} are calibrated to measurement data of engines that produce maximum nvPM mass emissions at take-off thrust. The models predict lowest nvPM mass emissions at idle and an exponential increase with increasing thrust. Thus, the nvPM emissions of the engine type investigated here cannot be well predicted using such a modeling approach without engine-specific SN or nvPM data.

Our nvPM measurements and modeled cruise emissions allowed comparison with previous studies of large engines at ground and at cruise. The ground level emission measurements have shown that the high thrust modes produced the lowest nvPM emissions, however, the low power conditions, which dominated the LTO cycle, produced up to an order of magnitude more nvPM mass and number than a Boeing 737 airliner. Consequently, taxiing aircraft with nvPM emission characteristics as found here may be an important pollution source at ground. Relatively high nvPM EIs were found also at cruise condition. If we expand the comparison with the Boeing 737 nvPM emissions\textsuperscript{31} to the overall flight emissions, during a 2-hour cruise and the regulatory LTO cycle, the business jet would produce 190 g of nvPM and $2.54 \times 10^{18}$ of particles, which is twice as much nvPM mass and \textasciitilde{}65% of the nvPM number of the airliner. Expressed as a per-person burden (assuming 180 airliner passengers and 5 business jet passengers), the nvPM mass emissions are higher by a factor of 72 and the nvPM number emissions are higher by a factor of 24.

These results highlight the need for further emissions research of small aircraft engines. To evaluate the applicability of our results, future studies should investigate nvPM mass and number emissions and size distributions as a function of engine thrust of different engine types to
develop emission inventories and more robust predictive models for ground and cruise
emissions. This study will serve for the development of emission inventories and the results
could also be used in the regulatory framework for assessing the emissions certification
requirements of small aircraft turbine engines.

ASSOCIATED CONTENT

Supporting Information. Fuel properties, engine test matrix, system loss correction factors,
engine performance model and cruise emission calculation.

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Notes

The authors declare no competing financial interest.

ACKNOWLEDGEMENTS

Funding was provided by the Swiss Federal Office of Civil Aviation (FOCA). We thank the
Swiss Air Force for providing the aircraft and facilities, namely Ralph Loosli, Thierry Dey,
Michael Lüthy (crew Bern), Thierry Roulin, Canisius Brodard, Bruno Carrard, Pierre Dubi,
Christian Guillaume, Christian Bangerter (crew Payerne). We thank Rudy Dudebout from
Honeywell Aerospace for providing engine performance data. We thank MeteoSwiss for the
meteorological data. Thanks to Dr. Jacinta Edebeli for proofreading the article.
REFERENCES


Figure 1

184x160mm (300 x 300 DPI)
Figure 2

82x114mm (300 x 300 DPI)
Figure 3

82×114mm (300 x 300 DPI)
Figure 4

82x114mm (300 x 300 DPI)
Figure 5

177x82mm (300 x 300 DPI)